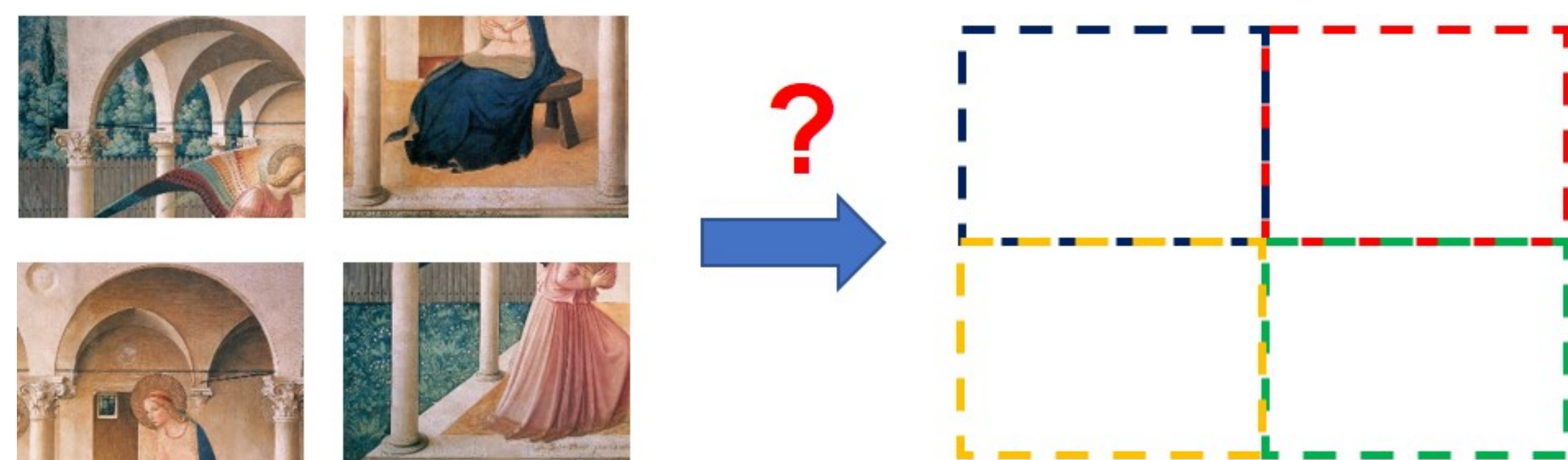




## 1. The Problem

Given a set of pieces (non-overlapping squares patches of an image) in a random configuration to infer the correct permutation to recover the original image.

**Challenge:** To overcome the combinatorially complex of matching adjacent pieces

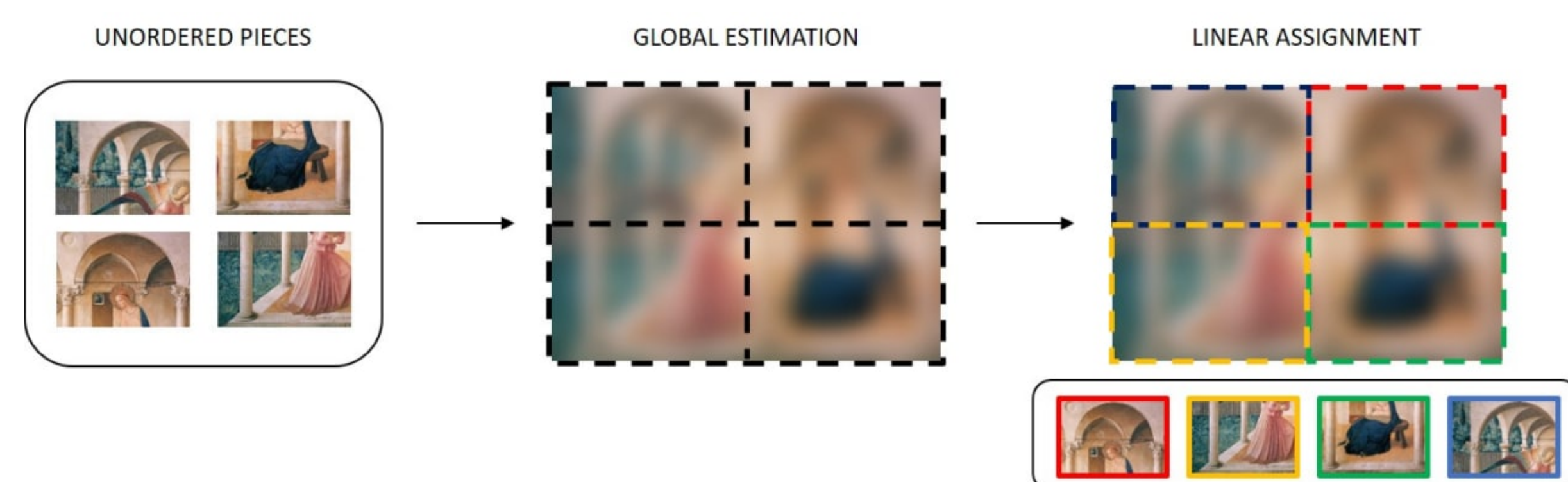


**Prior work:** Solving for adjacent pieces, *optimization-based* approaches [1] are time demanding and sensitive to initialization seed and erosion. *Deep Learning* approaches [7] are faster but do not generalize to multiple sizes.

## 2. Contribution

Exploiting advancements in Generative Adversarial Network (GAN) methods, we learn to estimate a global solution (mental image) to the problem from unordered pieces. Therefore, we frame the problem as a  $R@1$  retrieval task, and then solve the linear assignment using differentiable Hungarian Attention [7].

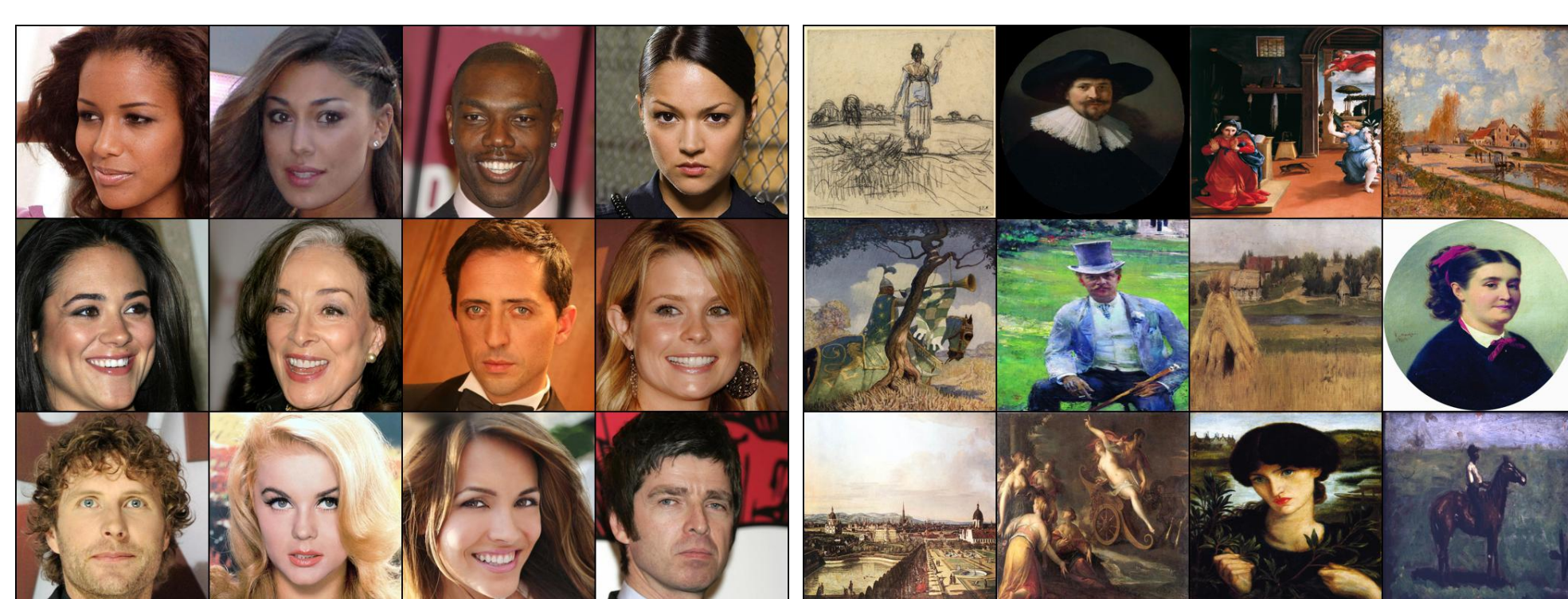
**TLDR;** Estimate the global solution (mental image). Match pieces against it.



- A **many-to-one GAN Architecture** for recovering a global image from its pieces.
- **Dynamic size puzzle solver** using Hungarian attention and contrastive loss.
- **Two new large-scale puzzle solving datasets**, named *PuzzleCelebA* [3] and *PuzzleWikiArts* [6], permutations are available for direct comparison.

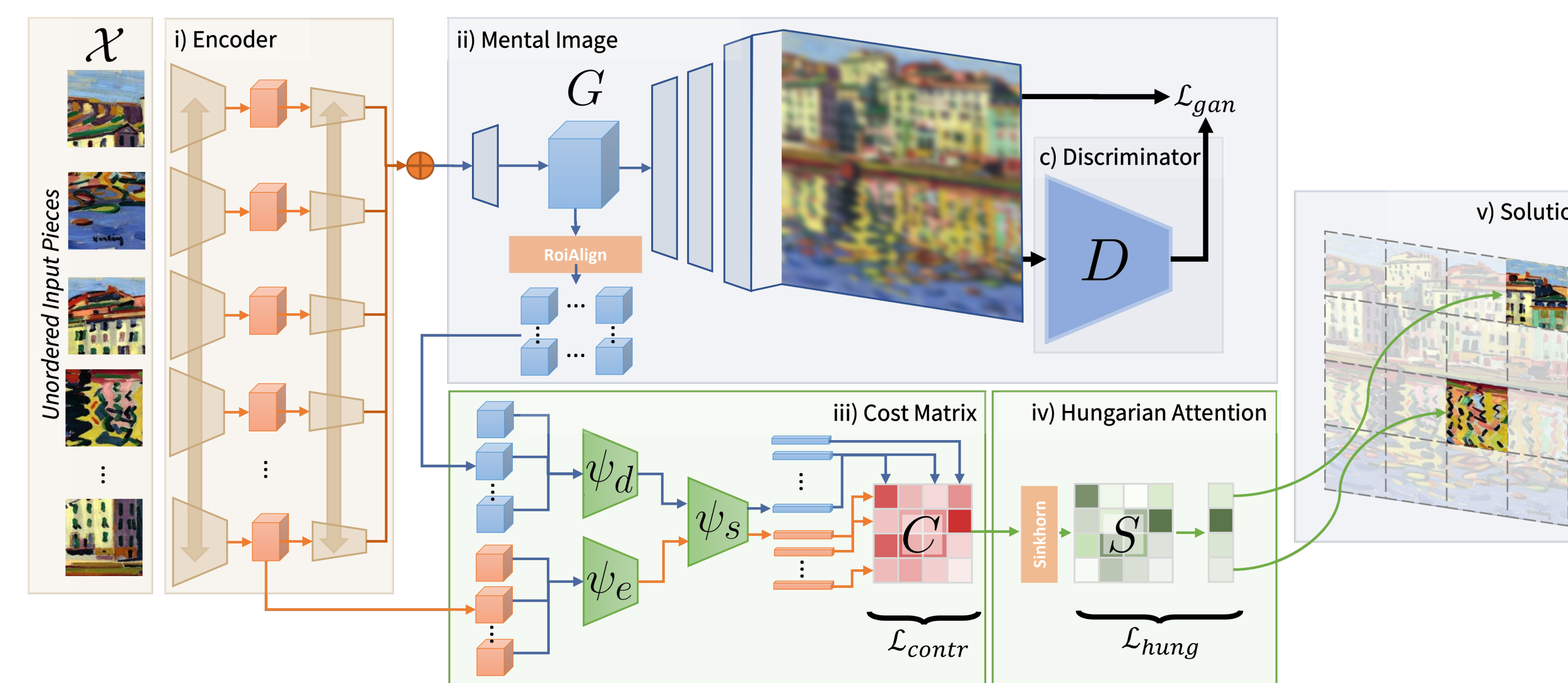
## 3. Dataset

The proposed benchmark builds on (left) *PuzzleCelebA* (30k images) and (right) *PuzzleWikiArts* (63k images), providing permutation of pieces at different puzzle sizes.



## 4. Architecture

Unordered pieces ( $\mathcal{X}$ ) are independently encoded and then pooled to produce a latent vector, from which the global solution (mental image) is estimated. After RoiAlign, generator intermediate features are used as global representation slots to be matched against. A cost matrix evaluates the piece to global slot similarity. Hungarian attention solves for the final permutation.



## 5. Key blocks

**Many-to-one GAN:** unordered pieces are encoded independently. The set of encodings is merged using average pooling to generate a single encoding vector. Then, a decoder projects back to the image space trained using adversarial and reconstruction loss for Multi-Scale Gradients [2].

**Cost matrix and contrastive loss:** the similarity matrix is computed as dot product of all possible piece-slot pairs. A contrastive loss enforces the feature space to have similar embeddings for piece-slot correct pairs while pushing apart non-corresponding pairs:

$$\mathcal{L}_{contr} = -\mathbb{E}_i \left[ \log \frac{\exp(\psi_s^i \cdot \psi_s^j / \tau)}{\exp(\psi_s^i \cdot \psi_s^j / \tau) + \sum_{k \neq j} \exp(\psi_s^i \cdot \psi_s^k / \tau)} \right] \quad (1)$$

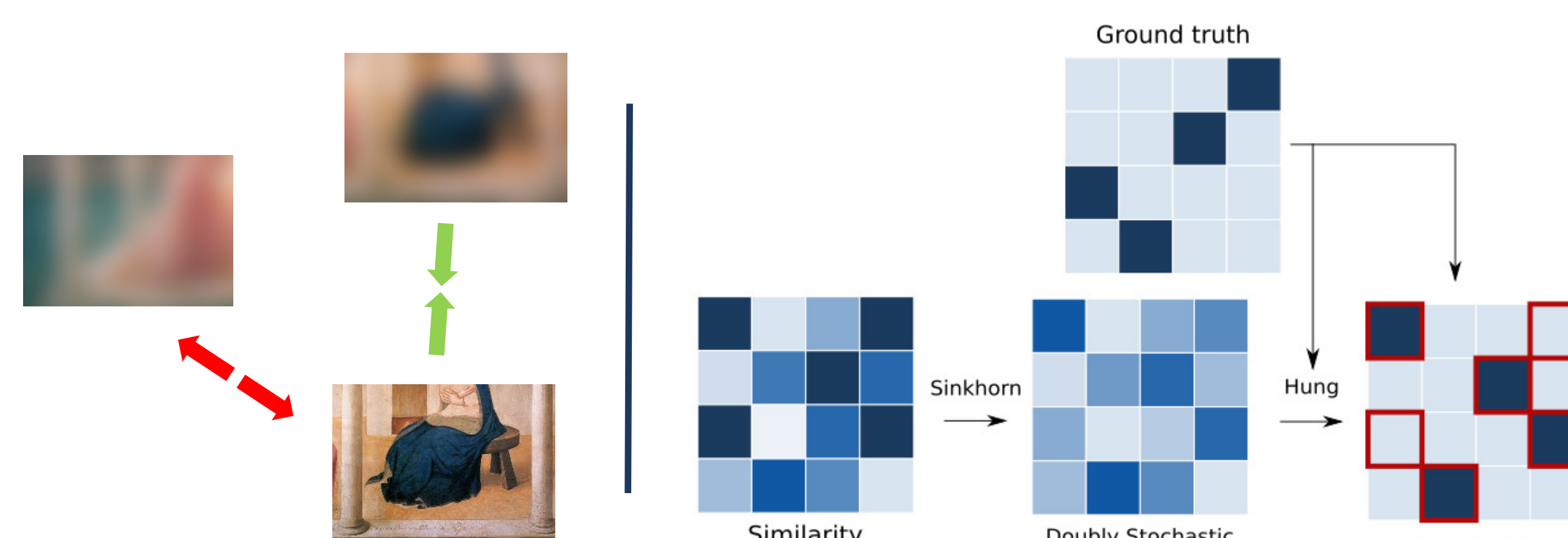
with  $\psi_s^i$  and  $\psi_s^j$  embeddings of considered piece  $i$  and  $j$  its corresponding slot.

**Hungarian attention (HA):** enables supervised learning of optimum assignments. The Sinkhorn normalization relaxes the cost matrix  $C$  to a doubly stochastic matrix  $S$ . Here, both correct and misplaced pieces are attended:

$$\mathbf{Z} = OR(\text{Hung}(S), S^G) \quad (2)$$

Binary cross-entropy loss with respect to the ground-truth  $S^G$  assignment matrix is attended through the mask  $\mathbf{Z}$ :

$$\mathcal{L}_{hung} = \sum_{i,j \in [n]} \mathbf{z}_{ij} \left( \mathbf{s}_{ij}^G \log \mathbf{s}_{ij} + (1 - \mathbf{s}_{ij}^G) \log (1 - \mathbf{s}_{ij}) \right), \quad (3)$$



(a) Contrastive Loss

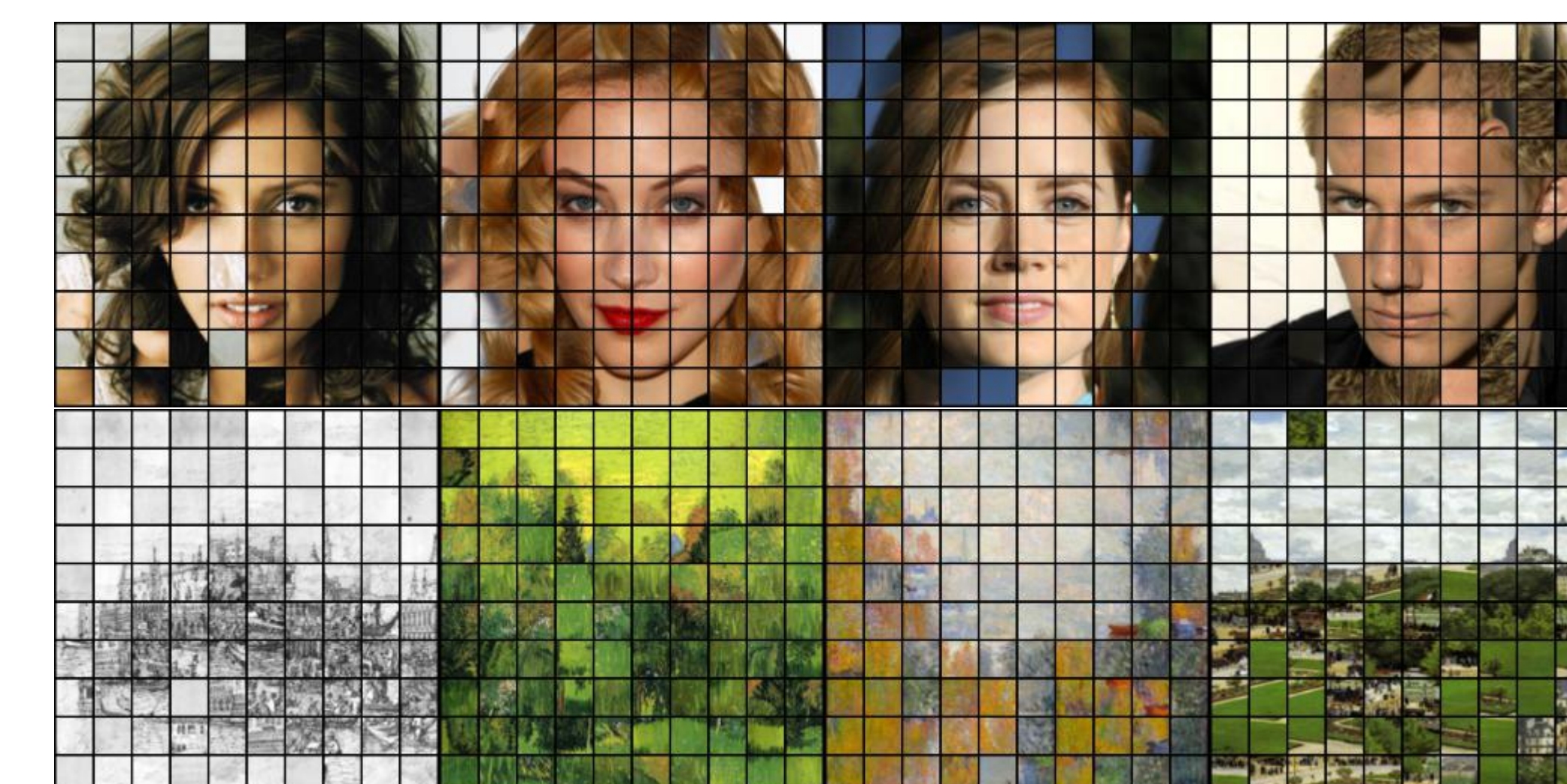
(b) Hungarian Attention

## 6. Results

Our method handles different sizes while performing on par with deep learning single-size approaches in terms of direct comparison accuracy.

| Dataset               | PuzzleCelebA |              |              |              | PuzzleWikiArts |             |             |             |
|-----------------------|--------------|--------------|--------------|--------------|----------------|-------------|-------------|-------------|
|                       | 6x6          | 8x8          | 10x10        | 12x12        | 6x6            | 8x8         | 10x10       | 12x12       |
| Paikin and Tal [4]    | 99.12        | 98.67        | 98.39        | 96.51        | 98.03          | 97.35       | 95.31       | 90.52       |
| Pomeranz et al. [5]   | 84.59        | 79.43        | 74.80        | 66.43        | 79.23          | 72.64       | 67.70       | 62.13       |
| Gallagher [1]         | 98.55        | 97.04        | 95.49        | 93.13        | 88.77          | 82.28       | 77.17       | 73.40       |
| PO-LA [8]             | 71.96        | 50.12        | 38.05        | -            | 12.19          | 5.77        | 3.28        | -           |
| Hung-perm             | 33.11        | 12.89        | 4.14         | 2.18         | 8.42           | 3.22        | 1.90        | 1.25        |
| GANzzle-Single (Ours) | 71.00        | 51.81        | <b>43.74</b> | -            | 11.78          | 6.23        | <b>8.97</b> | -           |
| GANzzle (Ours)        | <b>72.18</b> | <b>53.26</b> | 32.84        | <b>12.94</b> | <b>13.48</b>   | <b>6.93</b> | 4.10        | <b>2.58</b> |

Qualitative results of GANzzle for  $10 \times 10$  on (top) *PuzzleCelebA* and (bottom) *PuzzleWikiPaintings*



Limitations emerge with challenging pieces, i.e., pieces with similar content, as they can be interchangeable, however GANzzle is able to resolve for the structure of the image.

### Take home message

- It is possible to achieve state-of-the-art performances for puzzle problems of different sizes with a single trained model.
- Two benchmark datasets suitable for recent deep learning approaches are available for ease of comparison.
- Deep learning approaches are still far from optimization-based algorithms.

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